

attention and useful discussions.

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#### REGULAR REFLECTION OF AN OBLIQUE SHOCK IN A PLANE FLOW OF AN IDEALLY DISSOCIATING GAS IN THE PRESENCE OF A TRANSVERSE MAGNETIC FIELD

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R. RAM and V. D. SHARMA

(India)

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An oblique regular reflection is considered of a plane shock wave from a rigid wall in a steady flow of a perfect, ideally dissociating gas with infinite conductivity in the presence of a magnetic field normal to the plane of flow. A flow behind the reflected shock wave is studied in the vicinity of the triple point, i. e. the point at which the curvature of the shock wave becomes different from zero.

An assumption that a first order discontinuity occurs at the triple point, is used to obtain an expression for the jump in the derivatives of the flow parameters on the streamline emerging from this point and for the jumps in the current density and vorticity.

The properties of flow at the triple point regarded as a singularity on the reflected shock wave were first studied in [1]. Short conclusions derived from the theoretical papers dealing with the subject were given in [2]. Experimental data concerning the shock wave angles at the triple point were given in [3, 4]. Comparison of the theoretical and experimental results was presented in [5, 6], and [7, 8] analyse the Mach reflection. Theoretical and experimental results concerning the magnetohydrodynamic interaction between the reflected shock wave and a homogeneous magnetic field were given in [9].

The present paper represents a generalization of [10] to the case of an ideally conducting, dissociating gas in the presence of a transverse magnetic field.

**1. Statement of the problem.** The following simplifying assumptions are made: (1) viscosity, diffusion and heat conductivity are all neglected; (2) the dissociating gas is assumed diatomic and each of the reacting components is assumed to be a perfect gas; (3) the gas temperature varies from  $1000^\circ$  to  $7000^\circ$  K so that only the

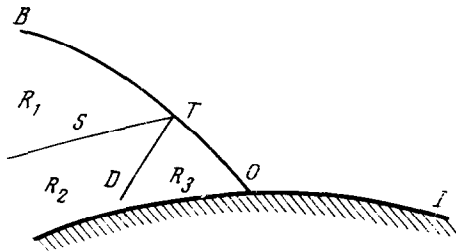


Fig. 1

process of dissociation is essential, the energy used on ionization and electron excitation being neglected and (4) the radiant energy losses are not taken into account.

The condition upstream of the incident rectilinear shock is assumed homogeneous, therefore the flow parameters in the region  $IOTB$  (see Fig. 1) can be assumed constant without loss of generality. The reflected shock becomes

curved behind the point  $T$  due to the effect of the sonic perturbations. The streamline  $ST$  emerging from the triple point  $T$  divides the region  $OTB$  lying behind the reflected shock wave into a region of homogeneous parameters behind the rectilinear part  $OT$  of the shock, and an inhomogeneous region ( $R_1$ ) behind the curved part  $TB$  of the shock.

At the point  $T$  the curvature of the shock suffers a discontinuity, although its first derivative remains continuous, i. e. the rectilinear part of the shock is tangent to the curved part at the point  $T$ . Further it is assumed that a first order discontinuity occurs at  $T$ . Then the conditions of continuity of the total pressure (magnetic plus gasdynamic), as well as continuity of streamline curvatures, hold at this point which lies on the streamline  $TS$ . To satisfy the last condition we shall assume, following [10], that the region behind the rectilinear part of the shock wave is divided by the curved boundary ( $TD$ ) into two parts: one part which is directly adjoint to the shock wave  $OTD$  ( $R_3$ ), in which all parameters are homogeneous, and the region  $STD$  ( $R_2$ ), in which the flow parameters vary continuously in a specific manner.

The equations of continuity, motion, energy and magnetic field induction for the case of a two-dimensional steady flow of an ideally conducting gas in the presence of a transverse magnetic field, are written in the form

$$\begin{aligned}
 u_i p_{,i} + \rho u_{i,i} &= 0 & (1.1) \\
 \rho u_j u_{i,j} + p_{,i}^* &= 0 \quad (p^* = p + H^2 / 8\pi) & (1.2) \\
 \rho u_i h_{,i} - u_i \rho_{,i} &= 0 & (1.3) \\
 u_i H_{,i} + H u_{i,i} &= 0 & (1.4)
 \end{aligned}$$

Here  $\rho, p, u_i$  and  $h = h(p, \rho, \alpha)$  are, respectively, the density, pressure, velocity components and total enthalpy of the mixture ( $\alpha$  is the degree of dissociation). The repeated index denotes summation over the region 1, 2 and a coma preceeding the index denotes differentiation with respect to the corresponding coordinate.

We shall consider the gas as a mixture formed by dissociation of a diatomic gas  $A_2$ , the molecules of which are composed of the atoms  $A_1$  of the gas. Assuming that the dissociation is ideal we shall write, following [11], the equations of state and an expression for the enthalpy, in the form

$$p = (1 + \alpha) \rho RT, \quad h = \frac{(4 + \alpha) p}{\rho (1 + \alpha)} + \alpha D \tag{1.5}$$

where  $T$  is temperature,  $R$  is the gas constant for  $A_2$  and  $D$  is the energy of dissociation. In this case, using the equation of continuity for  $A_1$  from [12], we obtain the following expression for the degree of dissociation

$$u_j \alpha_{,j} = \frac{4K_r \rho D^2 (1 + \alpha)}{R^2 T_d^2} \left[ \rho_d (1 - \alpha) \exp\left(-\frac{T_d}{T}\right) - \rho \alpha^2 \right] \tag{1.6}$$

Here  $\rho_d$  and  $T_d$  are the characteristic density and temperature obtained in [11] and  $K_r$  is the rate of the reverse reaction. Observations show that within the temperature range given above the quantity  $\rho_d$  varies little, therefore from now on we shall assume it constant. Inserting (1.1), (1.2), (1.5) and (1.6) into (1.3), we obtain

$$\begin{aligned}
 u_i p_{,i} + \rho a_f^2 u_{i,i} + F &= 0, \quad a_f^2 = p (4 + \alpha) / 3\rho & (1.7) \\
 F &= \frac{4\rho K_r D^2}{3R^2 T_d^2} \left[ \rho_d (1 - \alpha) \exp\left(-\frac{T_d}{T}\right) - \rho \alpha^2 \right] [\rho D (1 + \alpha)^2 - 3p]
 \end{aligned}$$

where  $a_f$  denotes the frozen speed of sound.

Let the equation of the reflected shock wave be given in the parametric form  $x_i = x_i(s)$  ( $i=1, 2$ ), where  $x_i$  is the Cartesian coordinate of the discontinuity and  $s$  is the arc length along this discontinuity. Any streamline intersecting the reflected shock can be defined as a curve  $s = \text{const}$ . Let  $\tau$  be the arc length along a streamline. Behind the reflected shock wave we pass to the curvilinear  $(s, \tau)$ -coordinate system in such a manner, that  $\tau = 0$  corresponds to the shock wave  $OTB$  (see Fig. 1). Let  $\lambda_i$  and  $n_i$  denote the components of the unit vector tangential and normal to the line  $\tau = \text{const}$ . Then we have the following relations [10]

$$\begin{aligned}
 \frac{\partial x_i}{\partial s} &= \lambda_i, \quad \frac{\partial x_i}{\partial \tau} = \frac{u_i}{v}, \quad v^2 = u_i u_i \\
 u_t &= u_i \lambda_i, \quad u_n = u_i n_i \\
 n_i &= e_{ij} \lambda_j \quad (e_{11} = e_{22} = 0, \quad e_{12} = -e_{21} = 1) & (1.8) \\
 f_{,i} &= \frac{\partial f}{\partial s} \frac{e_{ik} u_k}{u_n} + \frac{\partial f}{\partial \tau} \frac{v n_i}{u_n}
 \end{aligned}$$

Using (1.8) we now write (1.1), (1.2), (1.4) and (1.7) in the form

$$v \frac{\partial \rho}{\partial \tau} + \frac{\rho v}{u_n} n_i \frac{\partial u_i}{\partial \tau} - \frac{\rho}{u_n} e_{ij} u_j \frac{\partial u_i}{\partial s} = 0 \tag{1.9}$$

$$\rho v \frac{\partial u_i}{\partial \tau} - \frac{e_{ij} u_j}{u_n} \frac{\partial p^*}{\partial s} + \frac{v}{u_n} n_i \frac{\partial p^*}{\partial \tau} = 0 \tag{1.10}$$

$$\rho \frac{\partial H}{\partial \tau} = H \frac{\partial \rho}{\partial \tau} \tag{1.11}$$

$$v \frac{\partial p}{\partial \tau} - v a_f^2 \frac{\partial \rho}{\partial \tau} + F = 0 \tag{1.12}$$

**2. Properties of the flow behind the reflected shock wave.**

Theorem 1. Variations in the flow characteristics along the streamlines and along the curves  $\tau = \text{const}$  are connected by the following relations

$$v (u_n^2 - a_f^{*2}) \frac{\partial \rho}{\partial \tau} = \frac{\rho v}{H} \left( u_n^2 - a_f^{*2} \right) \frac{\partial H}{\partial \tau} = -\rho u_n e_{ij} u_j \frac{\partial u_i}{\partial s} - F - u_i \frac{\partial p^*}{\partial s} \tag{2.1}$$

$$v (u_n^2 - a_f^{*2}) \frac{\partial p}{\partial \tau} = a_f^2 \left( \rho u_n e_{ij} u_j \frac{\partial u_i}{\partial s} - u_i \frac{\partial p^*}{\partial s} \right) + F \left( \frac{H}{4\pi\rho} - u_n^2 \right) \tag{2.2}$$

$$\rho v \frac{\partial u_i}{\partial \tau} = \frac{e_{ij} u_j}{\partial s} \frac{\partial p^*}{\partial s} - \frac{n_i}{u_n a_f^2} \left[ v (a_f^*)^2 \frac{\partial p}{\partial \tau} - \frac{H^2 F}{4\pi\rho} \right] \tag{2.3}$$

$$(a_f^{*2} = a_f^2 + H^2 / 4\pi\rho)$$

Proof. Multiplying (1.10) by  $n_i$ , eliminating  $\partial p^* / \partial \tau$  and  $n_i \partial u_i / \partial \tau$  and using (1.9), (1.11) and (1.12), we obtain (2.1). Substitution of (2.1) into (1.12) and (1.10) yields (2.2) and (2.3).

Theorem 2. The gradients of the flow characteristics along the curvilinear boundary  $TD$  are given by  $u_{i,j} = Ln_i' n_j'$ ,  $H_{,j} = -HLn_j' / u_n'$

$$p_{,i} = L \left( \frac{H^2}{4\pi u_n'} - \rho u_n' \right) n_i', \quad \rho_{,i} = -\frac{\rho Ln_i'}{u_n'} \tag{2.5}$$

$$L = \frac{F}{\rho [(u_n')^2 - a_f^{*2}]}, \quad u_n' = u_i n_i' \tag{2.6}$$

where  $n_i'$  denote the components of a unit vector normal to the curve  $TD$ .

Proof. In the region  $R_3$  all parameters are constant, therefore at the boundary  $TD$  we have

$$u_{i,j} \lambda_j' = 0, \quad H_{,j} \lambda_j' = 0, \quad p_{,j} \lambda_j' = 0, \quad \rho_{,j} \lambda_j' = 0 \tag{2.7}$$

$$u_{i,j} = \beta_i n_j', \quad H_{,i} = \xi_i n_j', \quad \rho_{,i} = \zeta_i n_i' \tag{2.8}$$

Here  $\lambda_j'$  are the components of a unit vector tangent to  $DI$ . Multiplying (1.2) by  $\lambda_i'$ , using (2.7) and (2.8) and taking into account the fact that  $u_n' \neq 0$ , we have

$$\beta_i \lambda_i' = 0 \tag{2.9}$$

Eliminating  $u_i p_{,i}$  from (1.2) and (1.7), and using (1.4) and (2.8), we obtain

$$u_{i,i} = \beta_i n_i' = \frac{F}{\rho (u_n'^2 - a_f^{*2})} \equiv L \tag{2.10}$$

Comparing now (2.2) with (2.10), we conclude that

$$\beta_i = Ln_i' \tag{2.11}$$

Now we use (2.8) and (2.10) to obtain from (1.4) and (1.2)

$$\xi = -HL / u_n', \quad \zeta = -\rho L / u_n'$$

which proves the theorem.

Note. When the reaction is frozen,  $F = 0$  at every point of the flow. The flow in  $R_2$  is continuous and inhomogeneous, therefore from (2.4) – (2.6) it follows that  $L \neq 0$ , i. e. in  $R_2$  the following relation holds:

$$a_f^{*2} = u_n'^2$$

When  $F \neq 0$ , by virtue of (2.7), all quantities are continuous at the boundary and we therefore have on  $CD$

$$a_f^{*2} \neq u_n'^2$$

Theorem 3. The quantities in the region  $R_1$  and  $R_2$  are connected at the point  $T$  by the following relations:

$$\frac{vu_t}{u_n} \left( \frac{\partial p^*}{\partial \tau} \right)_{R_1} - \frac{v^2}{u_n} \left( \frac{\partial p^*}{\partial s} \right)_{R_1} = -\rho u_n' u_t' L \tag{2.12}$$

$$va_f^{*2} \left( \frac{\partial \rho}{\partial \tau} \right)_{R_1} = F - \rho L u_n'^2 \tag{2.13}$$

Proof. The curvature  $K$  of the streamline is given, with (1.2) taken into account, by

$$-v^3 K = e_{ik} u_k u_j u_{i,j} = \frac{1}{\rho} e_{ij} u_k p_{,i}^*$$

From this by virtue of the continuity of the curvature of the streamline at the point  $T$  we have

$$e_{ik} u_k(p, i^*)_{R_1} = e_{ik} u_k(p, i^*)_{R_2}$$

Expressing the pressure gradient in  $R_1$  in terms of the derivatives in  $\tau$  and  $s$  given by (1.8) and that in  $R_2$  using the formulas (2.4), (2.5), we obtain (2.12) at the point  $T$ . Here the derivative with respect to  $\tau$  of the total pressure in  $R_1$  is determined by (2.1) and (2.2). The variation of stream parameters along the curved part of the reflected shock wave can be expressed in terms of the wave intensity, curvature of the wavefront and the parameters of the free stream. Since the total pressure varies continuously along the streamline  $TS$ , we have

$$u_i(p, i^*)_{R_1} = u_i(p, i^*)_{R_2} \tag{2.14}$$

Using the relations (2.4) and (2.5) to express its right-hand side at  $T$  and (1.8) for its left-hand side, we obtain

$$v \left( \frac{\partial p^*}{\partial \tau} \right)_{R_1} = -\rho L u_n'^2 \tag{2.15}$$

Replacing now the left-hand side from (1.11) and (1.12), we obtain (2.13), Q.E.D.

Theorem 4. The jumps in the values of the gradients of the flow and magnetic field parameters on the streamline  $TS$  at the point  $T$ , are given by

$$[u_{,j}] = \frac{1}{v^2} \left\{ \frac{1}{\rho u_n} \left( e_{ik} u_k - \frac{u_t}{u_n} u_i \right) \left( \frac{\partial p^*}{\partial s} \right)_{R_1} + Lu_n' (n_i - n_i') \right\} u_j + \frac{1}{v^2} \left\{ Lu_n' n_i - Ln_t' n_i' - \frac{v^2}{u_n} \left( \frac{\partial u_t}{\partial s} \right)_{R_1} \right\} e_{jk} u_k \tag{2.16}$$

$$[H_{,i}] = \frac{H}{v^2} \{ (\rho a_f^{*2})^{-1} (F - \rho L u_n'^2) + L \} u_i +$$

$$\frac{1}{v^2} \left\{ H u_t (\rho u_n a_f^{*2})^{-1} (F - \rho L u_n'^2) - \frac{v^2}{u_n} \left( \frac{\partial H}{\partial s} \right)_{R_1} + \frac{u_t'}{u_n'} HL \right\} e_{vj} u_j \tag{2.17}$$

$$[p, i] = \frac{1}{v^2} \left\{ \frac{L}{4\pi} (4\pi u_n'^2 - H^2) - \frac{1}{a_f'^2} \left( \rho L u_n'^2 + \frac{H^2 F}{4\pi \rho} \right) \right\} u_i - \frac{1}{v^2} \left\{ \frac{v^2}{u_n} \left( \frac{\partial p}{\partial s} \right)_{R_1} + u_t (u_n a_f'^2)^{-1} \left( \rho L u_n'^2 a_f'^2 + \frac{H^2 F}{4\pi \rho} \right) + \frac{L u_t}{4\pi u_n'} (H^2 - 4\pi \rho u_n'^2) \right\} e_{ij} u_j \quad (2.18)$$

$$[\rho, i] = \frac{1}{v^2} \left\{ \rho L + \frac{1}{a_f'^2} (F - \rho L u_n'^2) \right\} u_i + \frac{1}{v^2} \left\{ u_t (u_n a_f'^2)^{-1} (F - \rho L u_n'^2) + \frac{\rho L u_t'}{u_n'} - \frac{v^2}{u_n} \left( \frac{\partial \rho}{\partial s} \right)_{R_1} \right\} e_{ij} u_j \quad (2.19)$$

Proof. Using the fact that the parameters are continuous on the streamline  $TS$ , we express the jumps in their derivatives at the point  $T$ , in the form

$$[f, i] = [a] u_i + [b] e_{ij} u_j \quad (2.20)$$

$$[a] = \frac{1}{v^2} \{ (u_i f, i)_{R_1} - (u_i f, i)_{R_2} \}$$

$$[b] = \frac{1}{v^2} \{ (e_{ij} u_j f, i)_{R_1} - (e_{ij} u_j f, i)_{R_2} \}$$

Here  $f$  denotes one of the quantities  $u_i, H, p$  or  $\rho$ , and the square brackets denote the corresponding jumps at the streamline  $TS$ . Using (2.4) – (2.6) we obtain the following expressions for the region  $R_2$  at the point  $T$ :

$$\begin{aligned} (u_j u_i, j)_{R_2} &= L u_n' n_i', & (e_{jk} u_k u_i, j)_{R_2} &= L u_t' n_i' \\ (u_i H, i)_{R_2} &= -HL, & (e_{ij} u_j H, i)_{R_2} &= -u_t' HL / u_n' \\ (u_i p, i)_{R_2} &= L \left( \frac{H^2}{4\pi} - \rho u_n'^2 \right), & (e_{ij} u_j p, i)_{R_2} &= L u_t' \left( \frac{H^2}{4\pi} - \rho u_n'^2 \right) \\ (u_i \rho, i)_{R_2} &= -\rho L, & (e_{ij} u_j \rho, i)_{R_2} &= -\rho L u_t' / u_n' \end{aligned} \quad (2.21)$$

Further, using the coordinate transformations (1.8), expressions (2.13) and Eqs.(1.10)–(1.12), respectively, we obtain the following expressions in the region  $R_1$ :

$$\begin{aligned} (u_j u_i, j)_{R_1} &= L u_n' n_i + \frac{1}{\rho u_n} e_{ij} u_j \left( \frac{\partial p^*}{\partial s} \right)_{R_1} \\ (e_{jk} u_k u_i, j)_{R_1} &= -\frac{v^2}{u_n} \left( \frac{\partial u_i}{\partial s} \right)_{R_1} + \frac{u_t}{u_n} \left\{ L u_n' n_i + \frac{1}{\rho u_n} e_{ij} u_j \left( \frac{\partial p^*}{\partial s} \right)_{R_1} \right\} \\ (u_i H, i)_{R_1} &= H (F - \rho L u_n'^2) (\rho a_f'^2)^{-1} \\ (e_{ij} u_j H, i)_{R_1} &= \frac{H u_t}{\rho u_n} \frac{(F - \rho L u_n'^2)}{a_f'^2} - \frac{v^2}{u_n} \left( \frac{\partial H}{\partial s} \right)_{R_1} + \frac{u_t'}{u_n'} HL \\ (u_i p, i)_{R_1} &= -\frac{1}{a_f'^2} \left( \frac{H^2 F}{4\pi \rho} + \rho L u_n'^2 a_f'^2 \right) \\ (e_{ij} u_j p, i)_{R_1} &= -\frac{u_t}{u_n a_f'^2} \left( \rho L u_n'^2 a_f'^2 + \frac{H^2 F}{4\pi \rho} \right) - \frac{v^2}{u_n} \left( \frac{\partial p}{\partial s} \right)_{R_1} \\ (u_i \rho, i)_{R_1} &= \frac{F - \rho L u_n'^2}{a_f'^2} & (e_{ij} u_j \rho, i)_{R_1} &= \frac{u_t (F - \rho L u_n'^2)}{u_n a_f'^2} - \frac{v^2}{u_n} \left( \frac{\partial \rho}{\partial s} \right)_{R_1} \end{aligned} \quad (2.22)$$

Substituting (2.21) and (2.22) into (2.20), we obtain (2.16) – (2.19), Q. E. D.

Theorem 5. The jumps of vorticity  $\omega$  and the current density  $j$  on the streamline  $TS$  at the point  $T$  are given by the formulas

$$\begin{aligned}
[\omega] &= \frac{Lu'_n}{v^2} (u_n - u_t) - \frac{1}{\rho u_n} \left\{ u_i \left( \frac{\partial u_i}{\partial s} \right)_{R_1} + \left( \frac{\partial p^*}{\partial s} \right)_{R_1} \right\} \\
[J_i] &= \frac{H}{4\pi v^2} \{ (\rho a_f^{*2})^{-1} (F - \rho L u_n'^2) + L \} e_{ij} u_j - \\
\frac{1}{4\pi v^2} &\left\{ H u_t (F - \rho L u_n'^2) (\rho u_n a_f^{*2})^{-1} - \frac{v^2}{u_n} \left( \frac{\partial H}{\partial s} \right)_{R_1} + \frac{u'_t}{u'_n} H L \right\} u_i \\
\omega &= {}^{1/2} (u_{j,i} - u_{i,j}) e_{ij}, \quad j = e_j H_{ij} / 4\pi
\end{aligned} \tag{2.23}$$

Considering the jump of these values on the streamline  $TS$  at the point  $T$  and using the formulas (2.16) and (2.17), we obtain (2.23).

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